

# Science and technology prospects for ultra-cold atoms

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Nov. 2002

- Atom de Broglie wave sensors
- S&T impact
- BEC impact
- Correlated atom systems

# Atom de Broglie wave sensors

# Position information

Problem: How obtain precise position information without GPS?

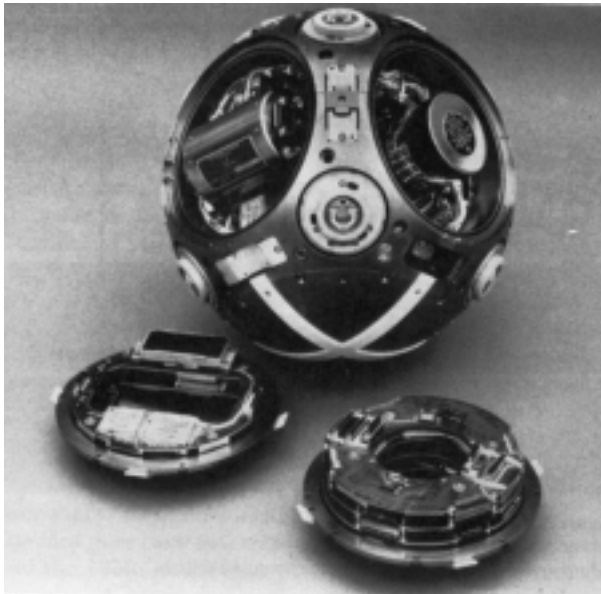
Next generation Inertial Navigation System (INS) solution: Improved INS may enable accurate global positioning without external reference signals

Current INS limitations:

- gyroscope drift (angle random walk)
- gravity compensation
- system cost and complexity

*Atom de Broglie-wave interference sensors address these current limitations*

# Existing high-accuracy technology



19,000 parts

\$300K/accelerometer in '89

1970 technology. 2001, 652  
units ordered.

Source: [www.fas.org](http://www.fas.org)

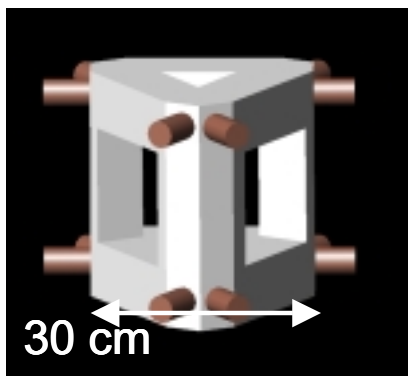
## Existing systems:

- Triad of gyroscopes (mechanical)
- Triad of accelerometers
- Precision gimbal mounts

# Gravity assisted-navigation with atom interferometric (AI) sensors

AI acceleration sensors offer breakthrough bias-stability and scale-factor stability

- enables high accuracy gravity gradiometry
- enables all-accelerometer-based gravity compensated navigation
- 3 year transition to field-tested systems. Leverage NIMA and Navy investments.



*Concept design for gravity compensated IMU*



*Cut-away view illustrating core sensor component: a Cs vapor cell. Not shown: control electronics.*

*Concept design for 2.75"x1.75",  $10^{-8}$  g/Hz<sup>1/2</sup> 2-axis accelerometer*



## AI sensor applications

### Gravity compensated navigation

Map-matching  
Real-time gravity anomaly correction for INS

### Gravity anomaly characterization

Underground facility detection

### Strategic platforms

Precision munitions  
Submarine/surface ship  
Land vehicles  
Helicopter/fixed wing aircraft  
ULDB Balloon flight  
Satellite constellation

### Commercial/civilian applications

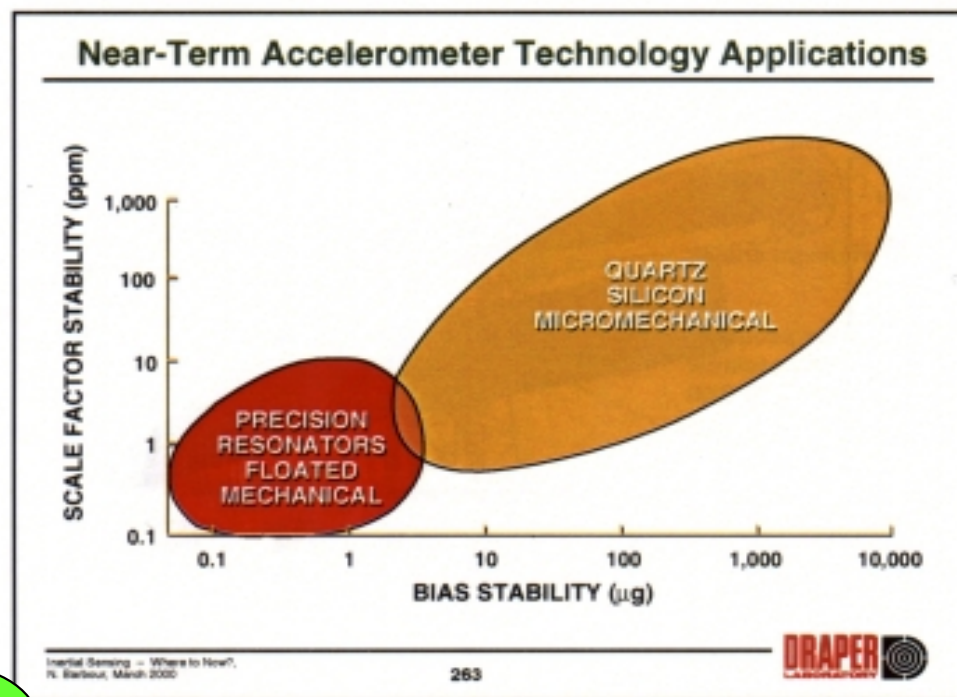
Satellite geodesy  
Earthquake prediction  
Water table monitoring  
Oil/mineral exploration

# Core sensor technology: High accuracy accelerometers

Light-pulse AI  
accelerometers:

Scale Factor  
stability:  $10^{-12}$

Bias stability:  
 $<10^{-10}$  g



AI

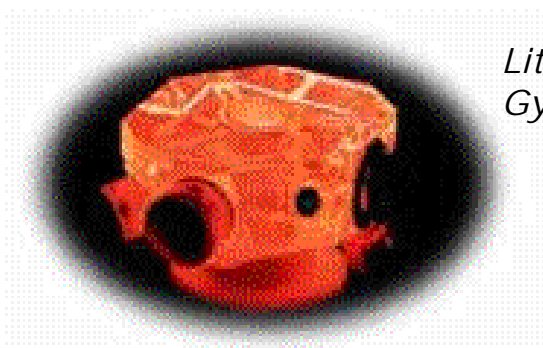
Source:IEEE PLANS 2000

*1000x improvement over state-of-the-art in these key sensor parameters.*

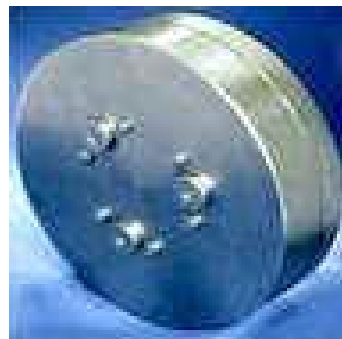
*Laboratory realizations at Stanford and Yale.*

# Interferometric sensors

## Optical Interferometry



*Litton Ring Laser Gyroscope*



*Fibersense Fiber-optic Gyroscope*

## Atom Interferometry

- Future atom optics-based sensors may outperform existing inertial sensors by a factor of  $10^6$ .
- Current (laboratory) atom optics-based sensors outperform existing sensors by a factor of  $10^2$ .



# Young's double slit with atoms

VOLUME 66, NUMBER 21 PHYSICAL REV

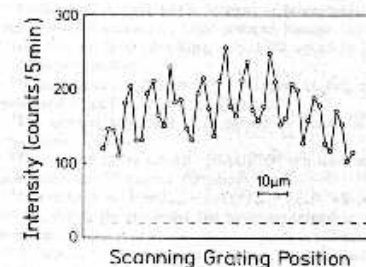
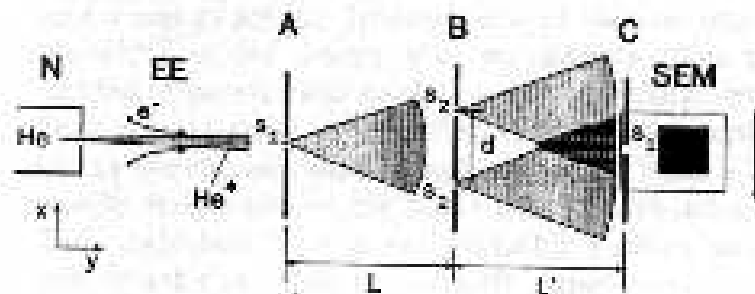
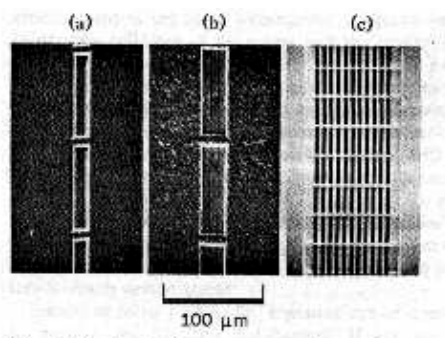


FIG. 5. Atomic density profile, monitored with the 8- $\mu\text{m}$  grating in the detector plane, as a function of the lateral grating displacement. The dashed line is the detector background. The line connecting the experimental points is a guide to the eye.

2691

*Young's 2 slit with Helium atoms*

*Interference fringes*



*Slits*

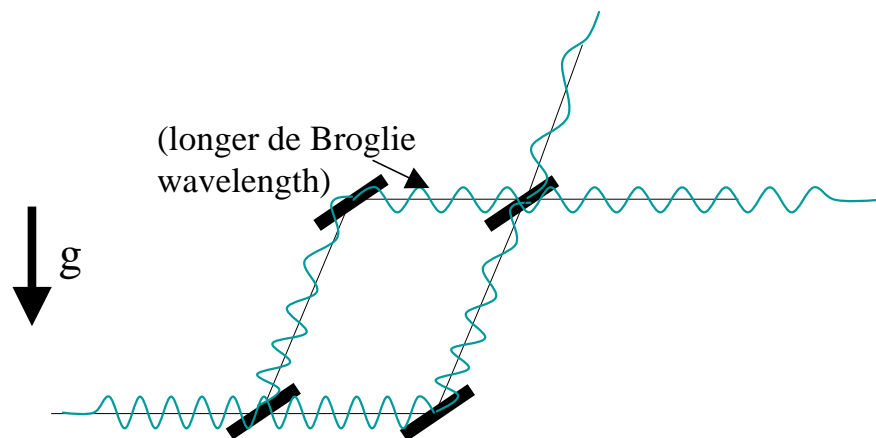
*One of the first experiments to demonstrate de Broglie wave interference with atoms, 1991*

# Atom interferometer force sensors

The quantum mechanical wave-like properties of atoms can be used to sense inertial forces.

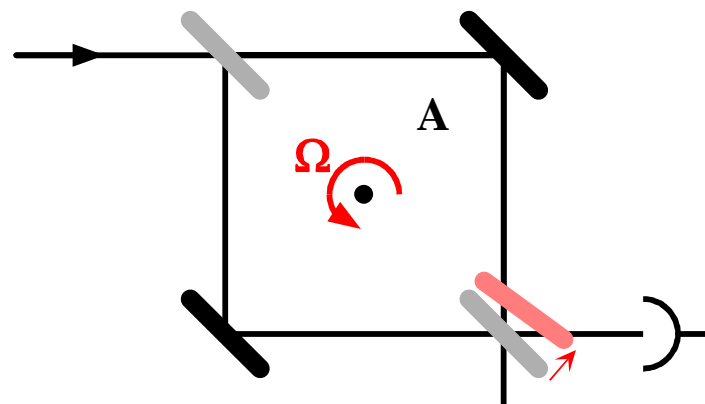
## Gravity/Accelerations

As atom climbs gravitational potential, velocity decreases and wavelength increases



## Rotations

Rotations induce path length differences by shifting the positions of beam splitting optics



# Enabling Science: Laser Cooling

*Laser cooling techniques are used to achieve the required velocity (wavelength) control for the atom source.*



Image source: [www.nobel.se/physics](http://www.nobel.se/physics)

**Laser cooling:**  
Laser light is used to cool atomic vapors to temperatures of  $\sim 10^{-6}$  deg K.



## The Nobel Prize in Physics 1997

"for development of methods to cool and trap atoms with laser light"



**Steven Chu**



USA  
Stanford University  
Stanford, CA, USA

1948 -



**Claude Cohen-Tannoudji**



France  
Collège de France  
Paris, France  
and École Normale Supérieure  
Paris, France

1933 -



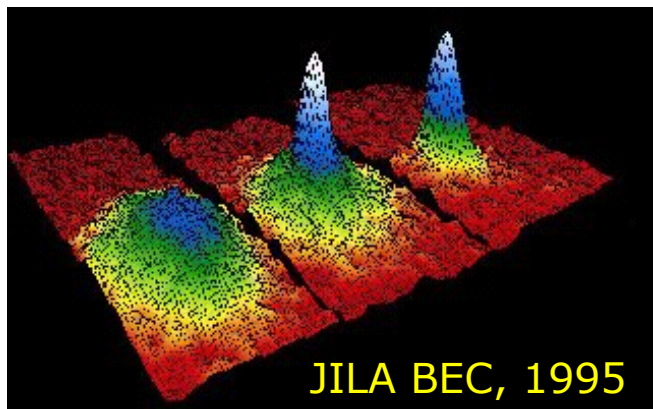
**William D. Phillips**



USA  
National Institute of Standards and Technology  
Gaithersburg, Maryland, USA

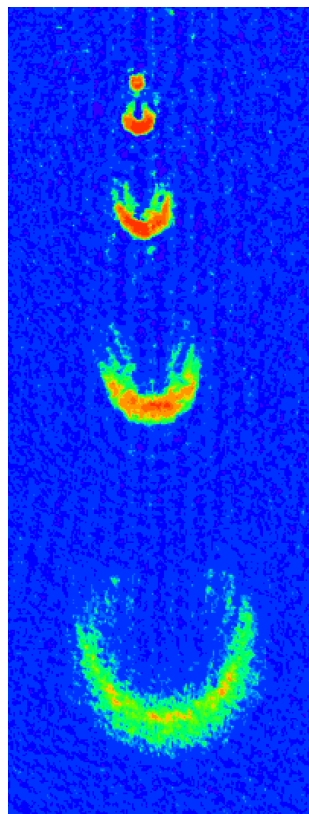
1948 -

# Enabling Science: BEC/Atom Lasers




Bose-Einstein  
Condensation of a dilute  
Rb atomic vapor







1<sup>st</sup> Atom  
Laser, MIT



*Revolution in production of bright,  
coherent atomic sources*

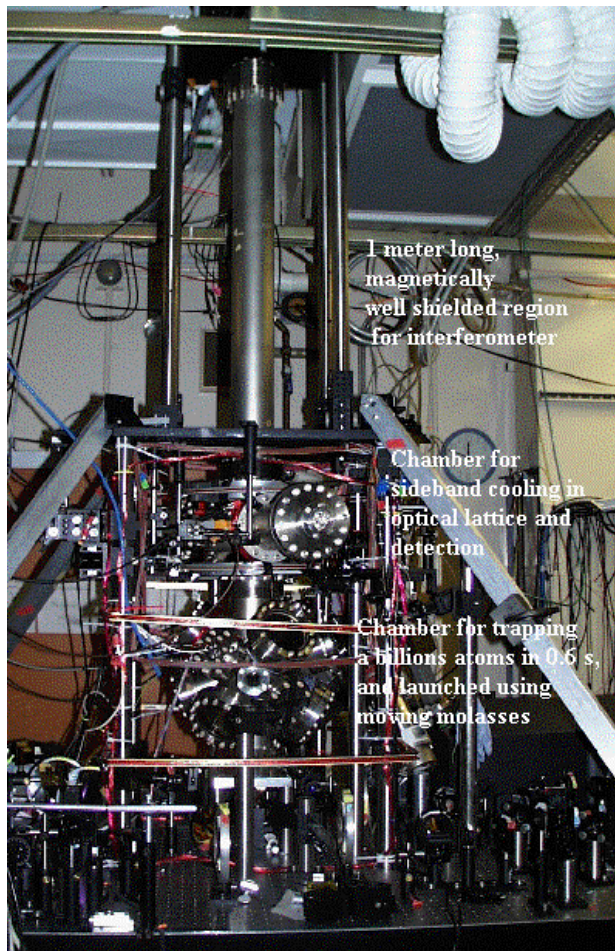
 **The Nobel Prize in Physics 2001**

"for the achievement of Bose-Einstein condensation in dilute gases of alkali atoms, and for early fundamental studies of the properties of the condensates"

 University of Colorado at Boulder	 MIT	 University of Colorado at Boulder
<b>Eric A. Cornell</b>	<b>Wolfgang Ketterle</b>	<b>Carl E. Wieman</b>
 USA	 Germany	 USA
JILA and National Institute of Standards & Technology (NIST) Boulder, CO, USA	Massachusetts Institute of Technology (MIT) Cambridge, MA, USA	JILA and University of Colorado Boulder, CO, USA
1961 -	1957 -	1951 -

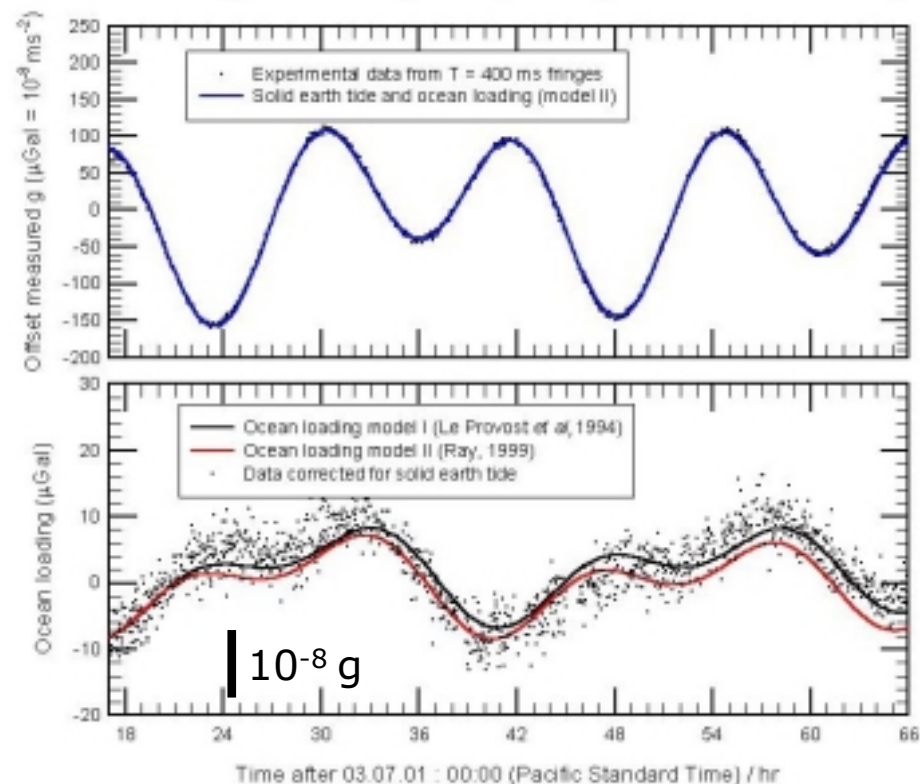
**2001 Nobel Prize!**

# Stanford laboratory gravimeter



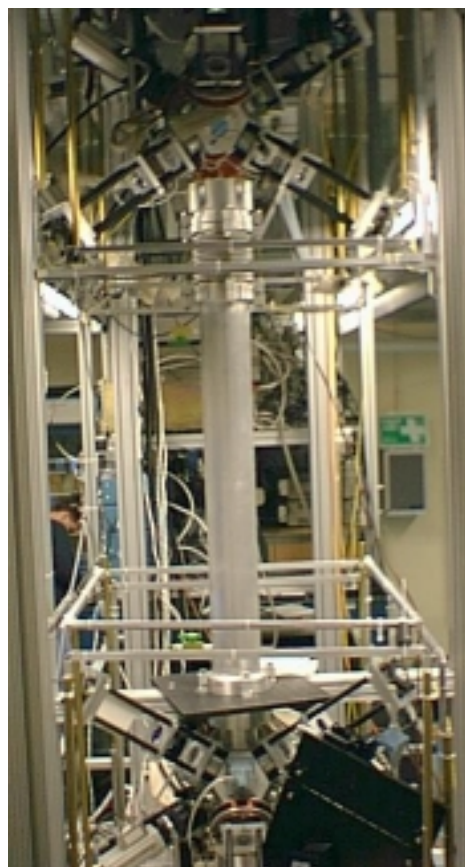
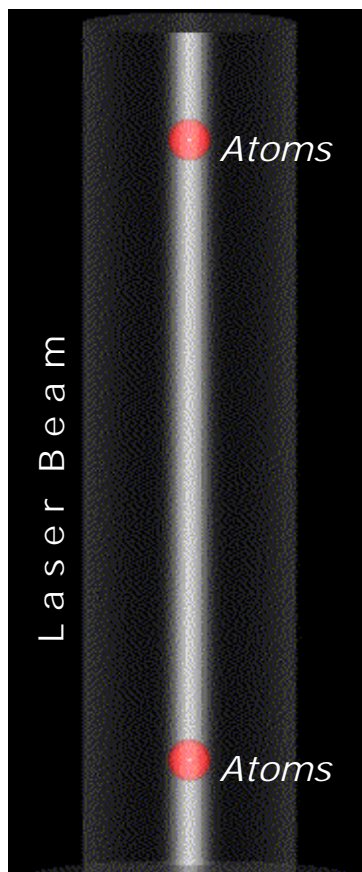
*Courtesy of S. Chu,  
Stanford*

Monitoring of local gravity using  $T = 400$  ms fringes

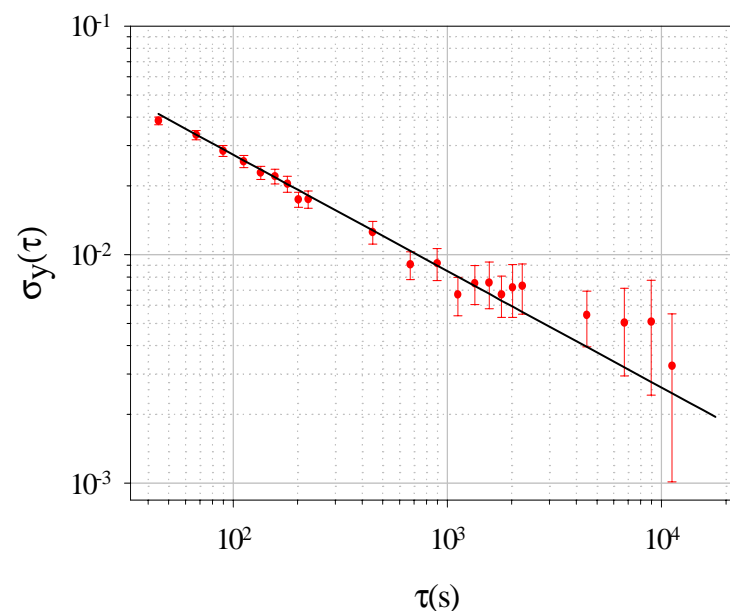


Raman sideband cooling used to achieve very long interrogation times (200 nK launch temperature!)

# Stanford/Yale laboratory gravity gradiometer



1.4 m



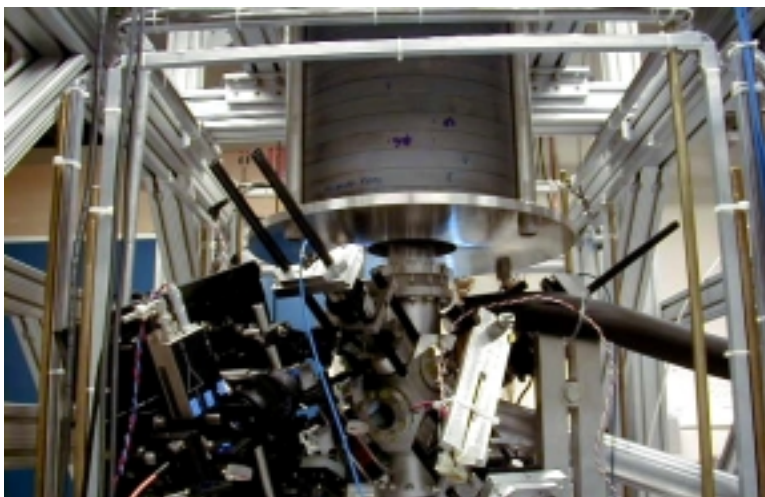
Demonstrated differential  
acceleration sensitivity:

$$4 \times 10^{-9} \text{ g/Hz}^{1/2}$$

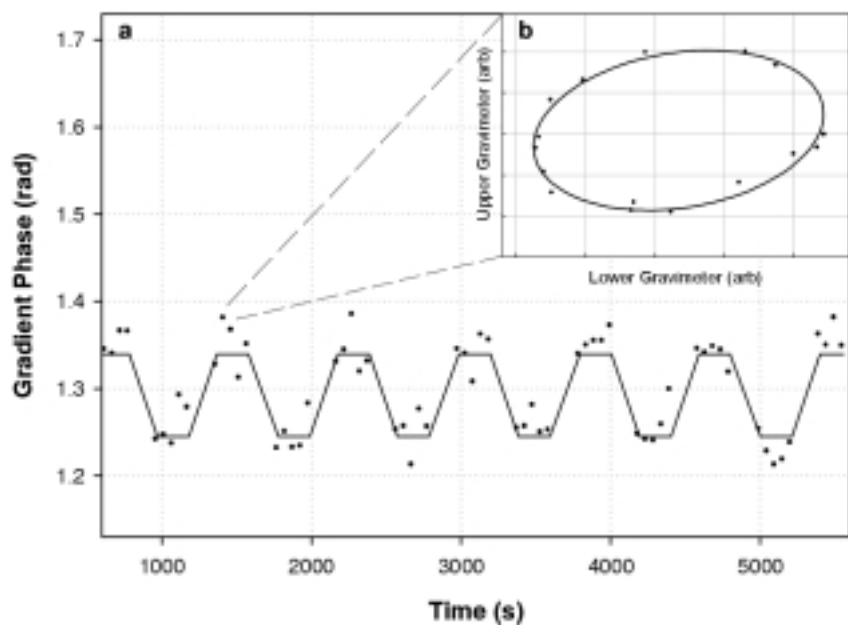
( $2.8 \times 10^{-9} \text{ g/Hz}^{1/2}$  per  
accelerometer)

*Distinguish gravity induced  
accelerations from those due to  
platform motion with differential  
acceleration measurements.*

# Stanford/Yale Gravity Gradiometer: Measurement of G



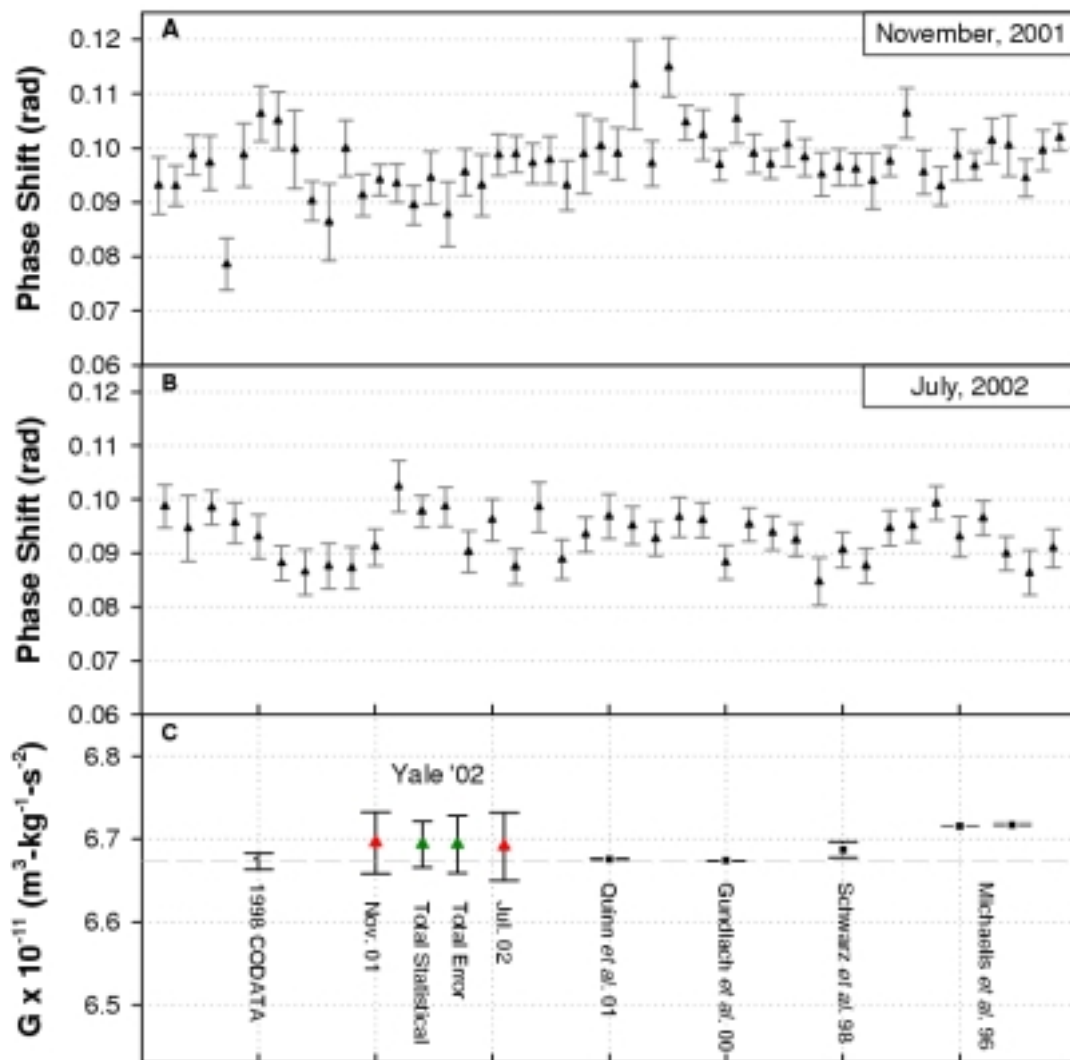
Pb mass translated vertically along gradient measurement axis.



*Typical data:*

*$\sim 1 \times 10^{-8}$  g change in acceleration due to gravitational forces for different Pb positions*

# Measurement of G



Systematic	$\frac{\delta G}{G}$
Initial Atom Velocity	$1.88 \times 10^{-3}$
Initial Atom Position	$1.85 \times 10^{-3}$
Pb Magnetic Field Gradients	$1.00 \times 10^{-3}$
Rotations	$0.98 \times 10^{-3}$
Source Positioning	$0.82 \times 10^{-3}$
Source Mass Density	$0.36 \times 10^{-3}$
Source Mass Dimensions	$0.34 \times 10^{-3}$
Gravimeter Separation	$0.19 \times 10^{-3}$
Source Mass Density inhomogeneity	$0.16 \times 10^{-3}$
<b>TOTAL</b>	<b><math>3.15 \times 10^{-3}</math></b>

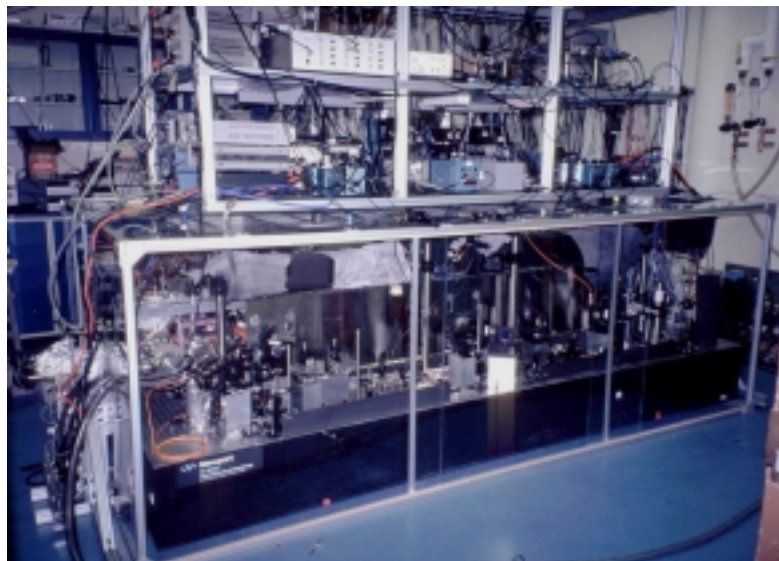
*Present sensitivity/accuracy:*

$$\delta G = 3 \times 10^{-3} G$$

*Measurement consistent with accepted value*



# Stanford/Yale laboratory gyroscope

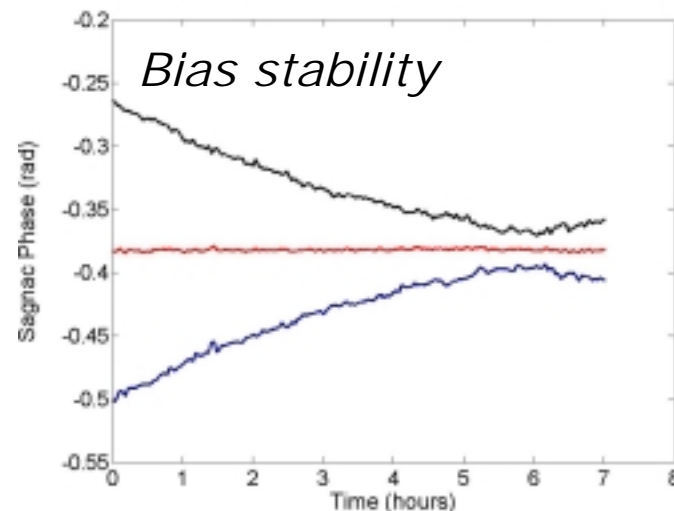
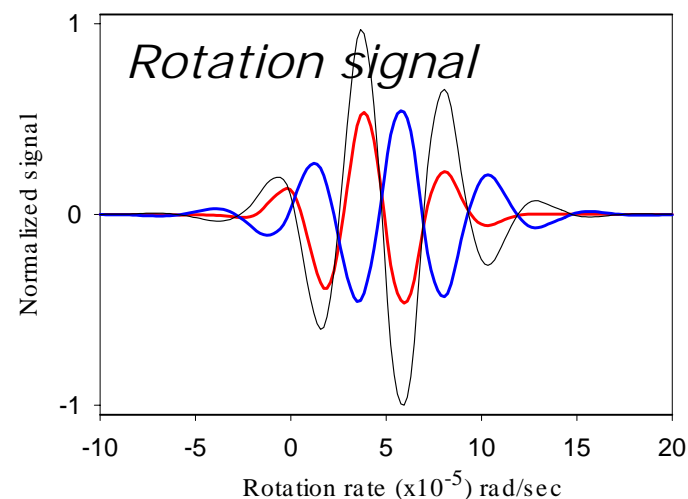


AI gyroscope, demonstrated laboratory performance:

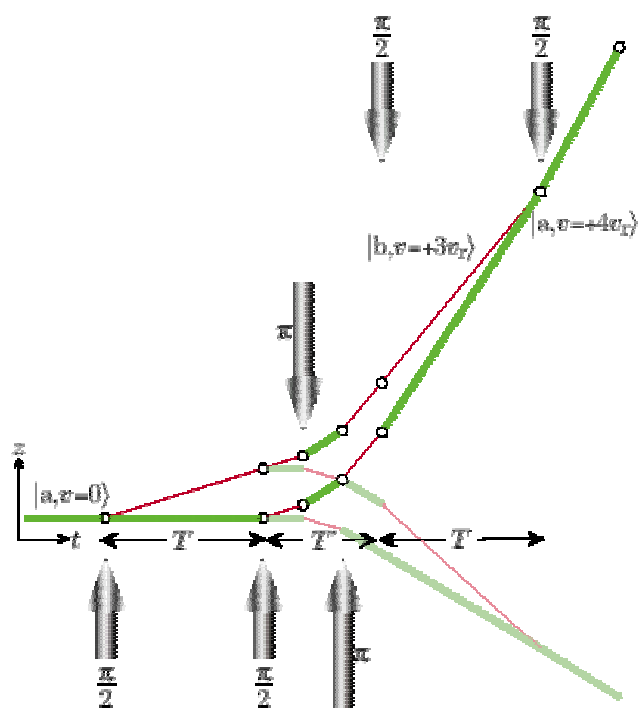
$2 \times 10^{-6}$  deg/hr<sup>1/2</sup> ARW

$< 10^{-4}$  deg/hr bias stability

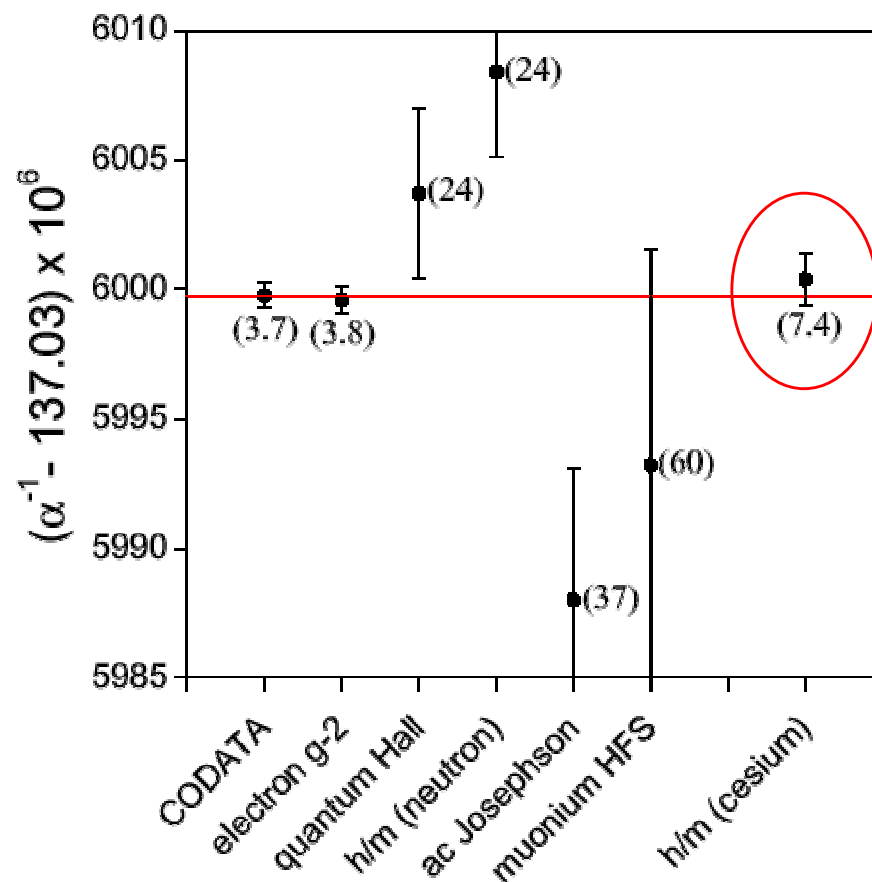
*Compact, fieldable (navigation) and dedicated very high-sensitivity (Earth rotation dynamics, tests of GR) geometries possible.*



# Stanford h/m



*Courtesy of S. Chu,  
Stanford (talk by A.  
Wicht, Wednesday)*



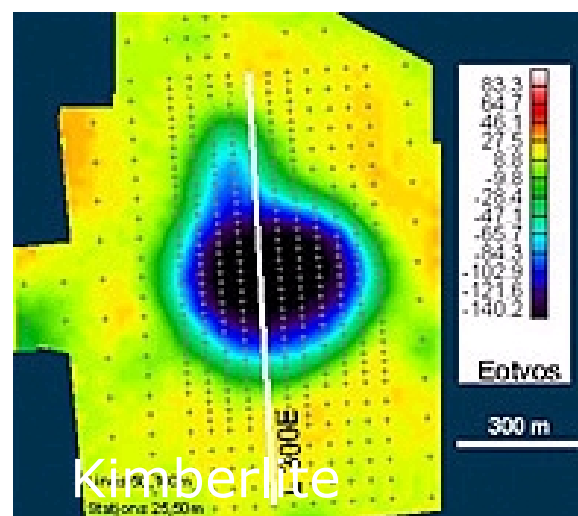
# Science and Technology Applications

# Airborne GG validation: BHP FALCON program

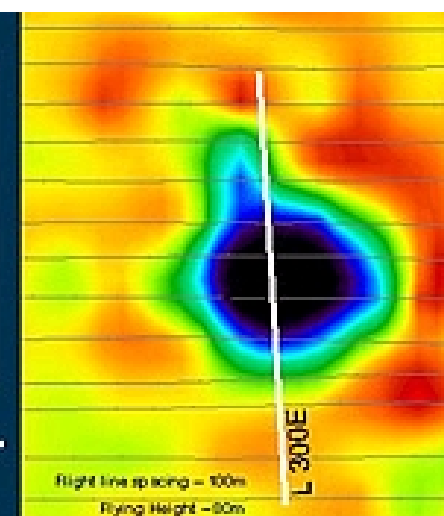
## Existing technology



Land: 3 wks.



Air: 3 min.

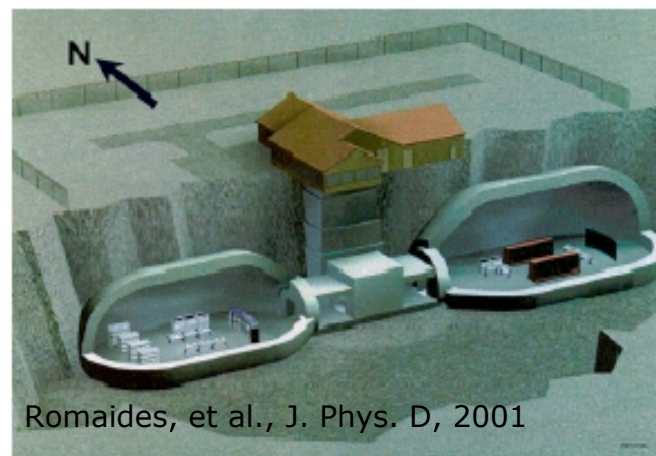


*All sensors potentially offer 10 x – 100 x improvement in detection sensitivity at reduced instrument costs.*

# Underground structure detection

*Gravity gradiometers can detect underground structures via their gravitational signatures.*

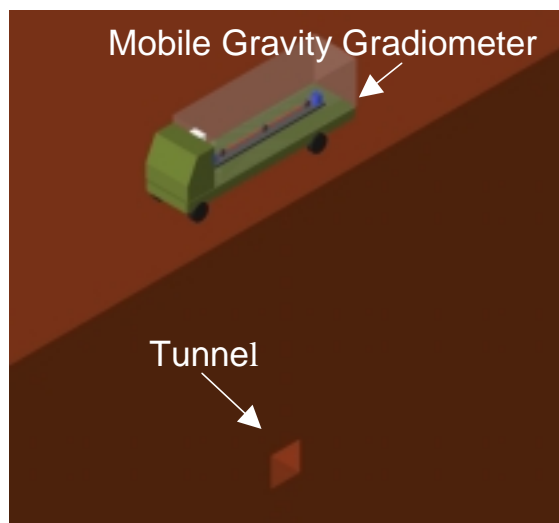
*AI appears to be sole sensor technology capable of meeting stringent sensitivity and accuracy requirements.*



Strategic moving platforms for gravity gradiometry:

- Helicopter/UAV platform
- Satellite reconnaissance (?)
- Truck

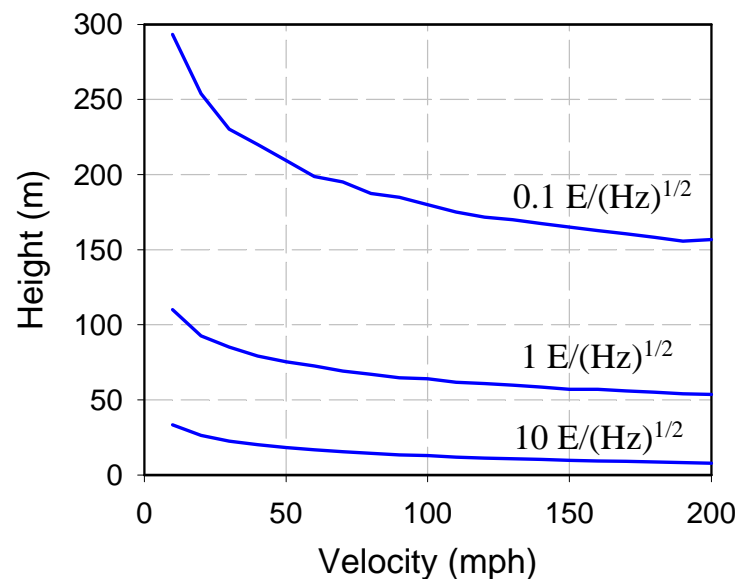
# Tunnel detection



Tunnel model:

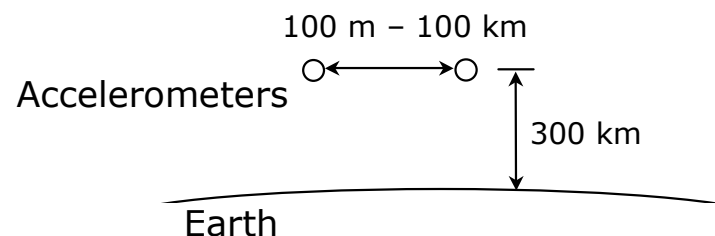
5 m x 5 m tunnel

$\delta\rho = 3 \text{ g/cm}^3$



*Field-ready  $1 \text{ E}/\text{Hz}^{1/2}$  instrument currently under development for truck/helicopter/aircraft platform*

# Geodesy



Accelerometer sensitivity:  $10^{-13}$  g/Hz<sup>1/2</sup>  
– Long free-fall times in orbit

Measurement baseline

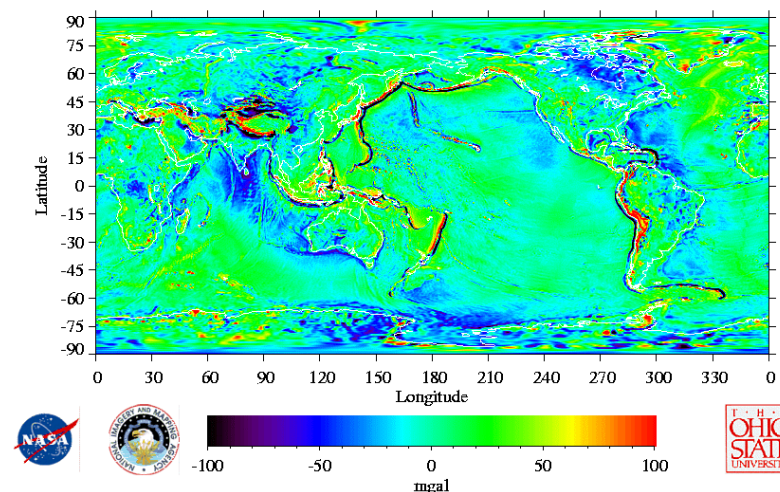
- 100 m (ISS)
- 100 km (Satellite constellation)

Sensitivity:

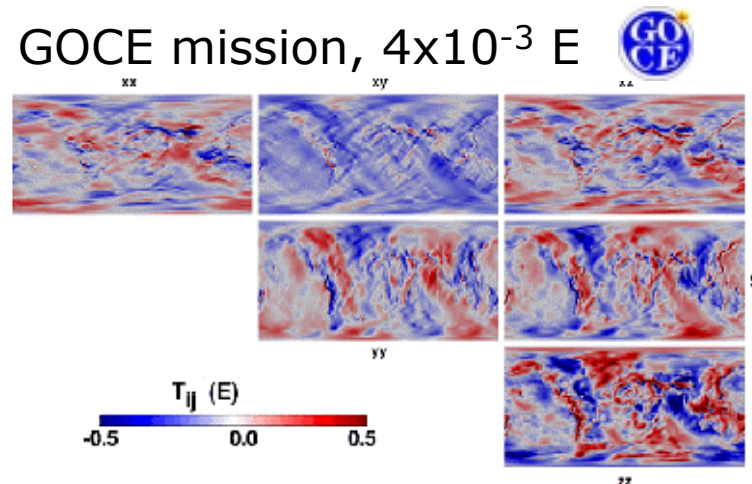
- $10^{-4}$  E/Hz<sup>1/2</sup> (ISS)
- $10^{-7}$  E/Hz<sup>1/2</sup> (Satellite constellation)

*Earthquake; water table monitoring  
(collaboration with T. Parsons, USGS)*

30' Mean Gravity Anomalies: EGM96 (Nmax=360)



GOCE mission,  $4 \times 10^{-3}$  E



<http://www.esa.int/export/esaLP/goce.html>

# Test of General Relativity

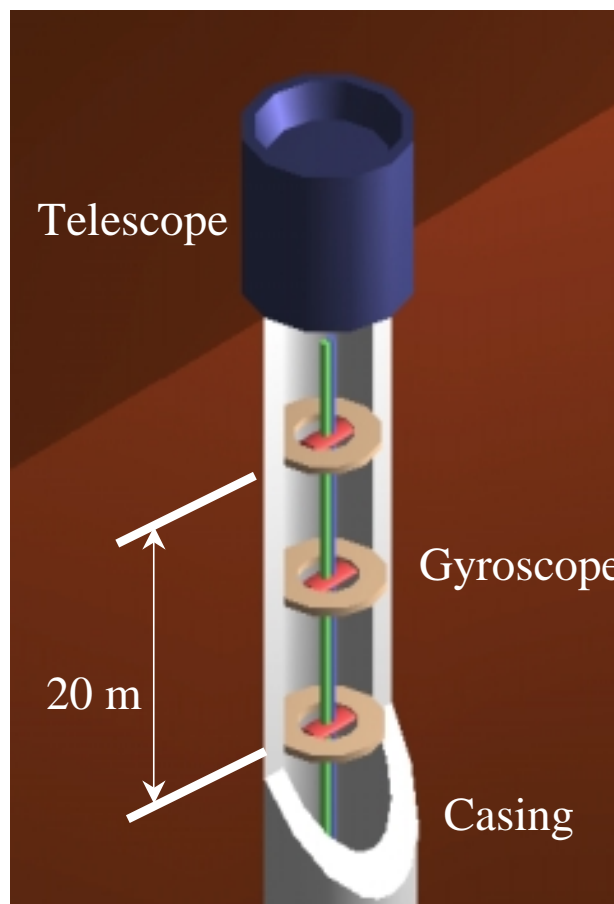
Lorentz-like force law:

$$\frac{d\vec{v}}{dt} = \vec{g} + \frac{\vec{v}}{c} \times \vec{H}$$

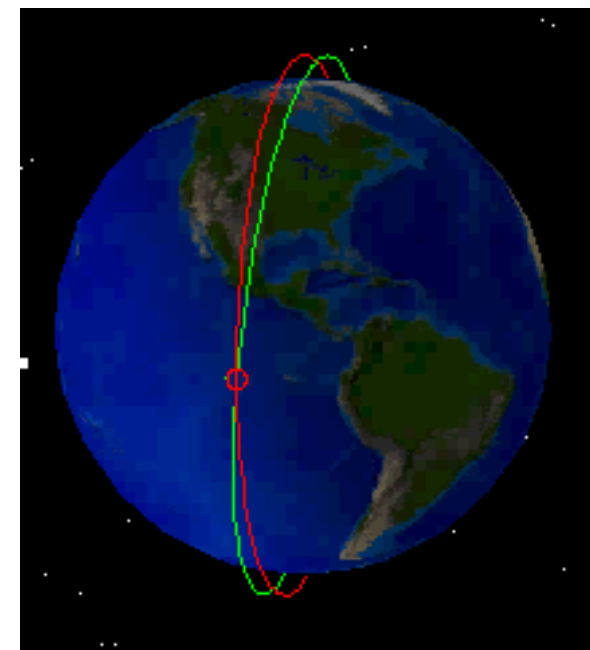
$$\vec{H} = \frac{2G}{c} \left[ \vec{S} - \frac{\vec{S} \cdot \hat{r}}{r^3} \hat{r} \right]$$

$S$  is angular momentum  
of rotating body

Basic idea: Compare  
rotation inferred from  
astrophysical observations  
to atom interferometer  
gyro signal.



*Ground-based*



*Satellite-based*

*$10^{-14}$  rad/sec rotation sensitivity required*



# Equivalence Principle

Compare relative acceleration of Cs and Rb atoms (or two Rb isotopes) using AI methods.

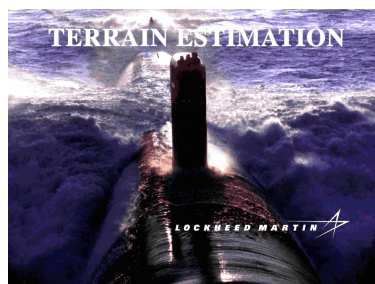
Constrain possible “new physics” beyond Standard Model at unprecedented levels.

$10^{-13}$  g/Hz<sup>1/2</sup> differential acceleration sensitivity appears feasible on ISS/free-flyer (in collaboration with L. Maleki, JPL through NASA Fund. Phys./flight definition)

RECENT theory: “Little String Theory at a TeV”, I. Antoniadis, S. Dimopoulos, A. Giveon, hep-th/0103033, 2002.

Dimopoulos: “More speculative than extra-dimensions....”

# Navigation

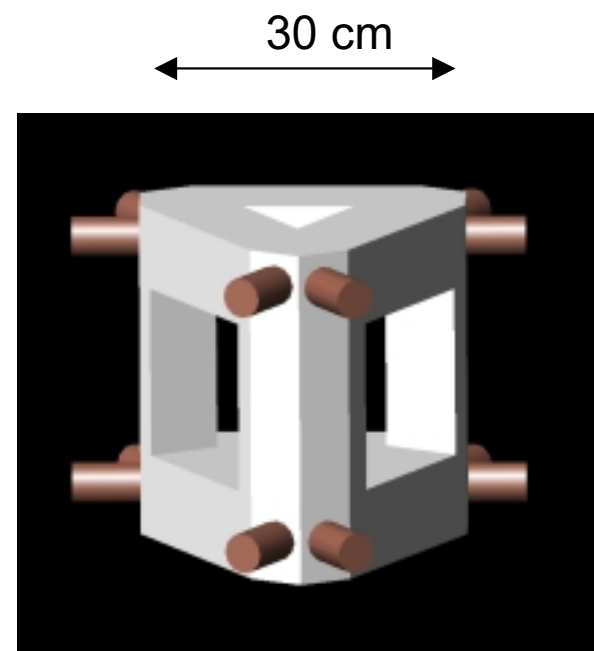


High-accuracy IMU with gravity compensation under development for Trident submarine navigation.

Array of 3-axis accelerometers on rigid platform

- In-line differential acceleration measurements along independent axes allow discrimination of angular accelerations from gravity gradients
- Integrate angular acceleration to correct for centrifugal perturbations

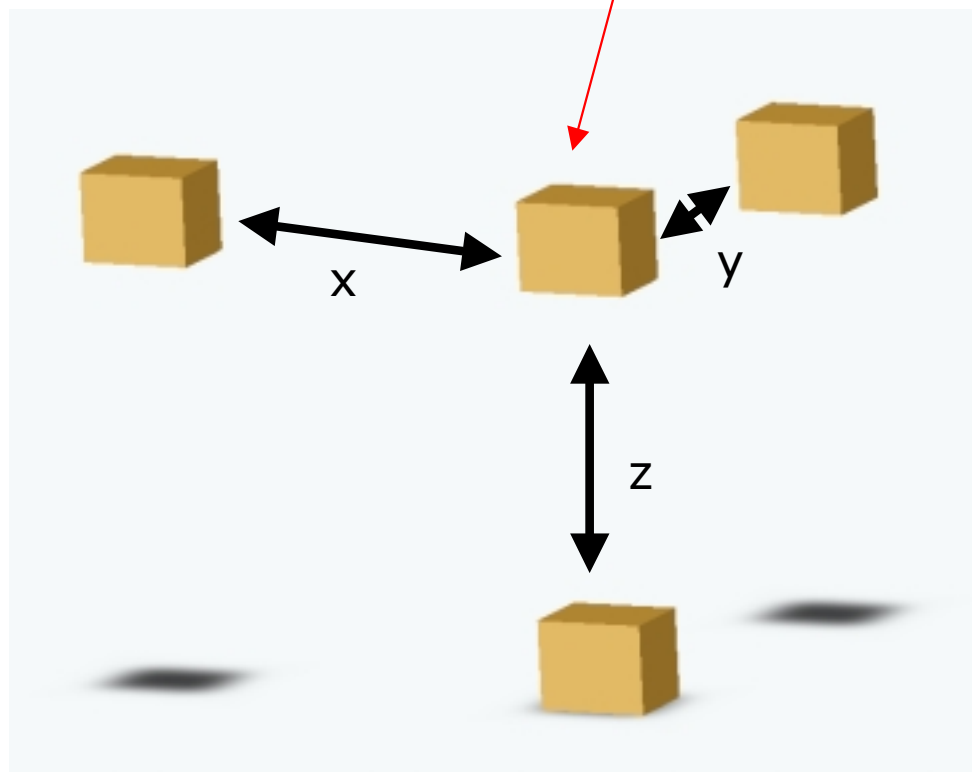
*Long-term vision: low-cost, high-reliability gravity compensated IMU's.*



*2<sup>nd</sup> generation proof-of-concept instrument.  
Brown = laser beams;  
Grey = vacuum cell*

# Navigation with accelerometer arrays

3-axis accelerometer  
(4 places)



Allows for gravity anomaly and platform position determination.

High accuracy gyroscopes may not be needed.

# Differential acceleration measurements

Differential acceleration measurements contains terms due to rotations and angular accelerations:

$$\begin{pmatrix} \mathbf{f}_{1x} - \mathbf{f}_{0x} \\ \mathbf{f}_{1y} - \mathbf{f}_{0y} \\ \mathbf{f}_{1z} - \mathbf{f}_{0z} \end{pmatrix} = \begin{bmatrix} -(\Gamma_{xx} + \Omega_y^2 + \Omega_z^2) \\ \dot{\Omega}_z - (\Gamma_{xy} - \Omega_x \Omega_y) \\ -\dot{\Omega}_y - (\Gamma_{xz} - \Omega_x \Omega_z) \\ -\dot{\Omega}_z - (\Gamma_{xy} - \Omega_x \Omega_y) & \dot{\Omega}_y - (\Gamma_{xz} - \Omega_x \Omega_z) \\ -(\Gamma_{yy} + \Omega_x^2 + \Omega_z^2) & -\dot{\Omega}_x - (\Gamma_{yz} - \Omega_y \Omega_z) \\ \dot{\Omega}_x - (\Gamma_{yz} - \Omega_y \Omega_z) & -(\Gamma_{zz} + \Omega_x^2 + \Omega_y^2) \end{bmatrix} \begin{pmatrix} \rho_x \\ \rho_y \\ \rho_z \end{pmatrix}$$

$\Gamma_{ij}$ : Gravity gradient

$\Omega_i$ : Rotation

$\rho_i$ : Displacement

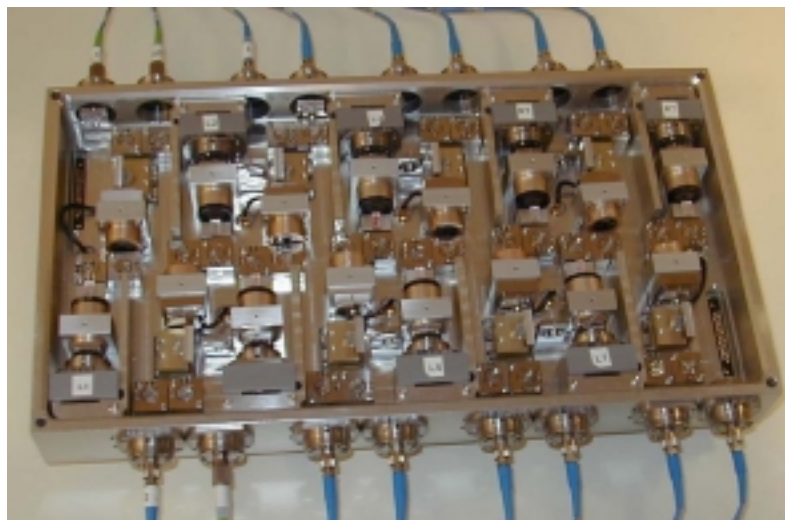
Accelerometer arrays enable high-accuracy navigation.

*See PLANS 2002, A. Zorn, Dynamics Research Corporation*

# Compact prototype under development

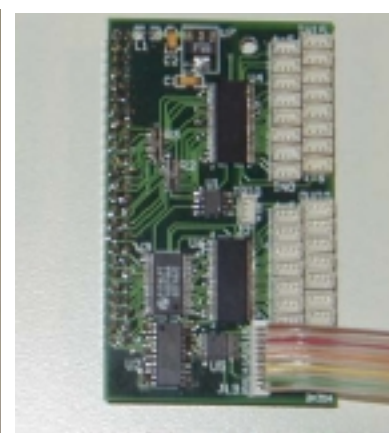


6dof motion testing platform

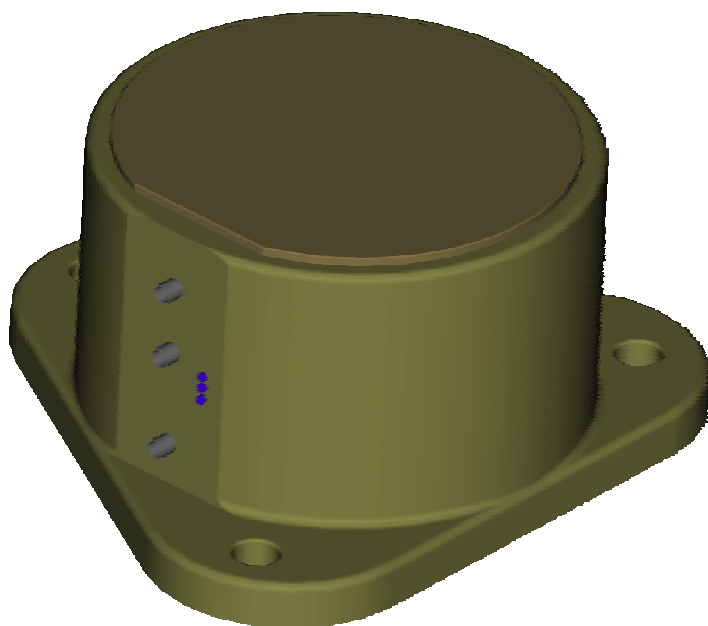


Component sub-systems under development

Field-ready prototype available FY03, est.



# Ground-based accelerometer



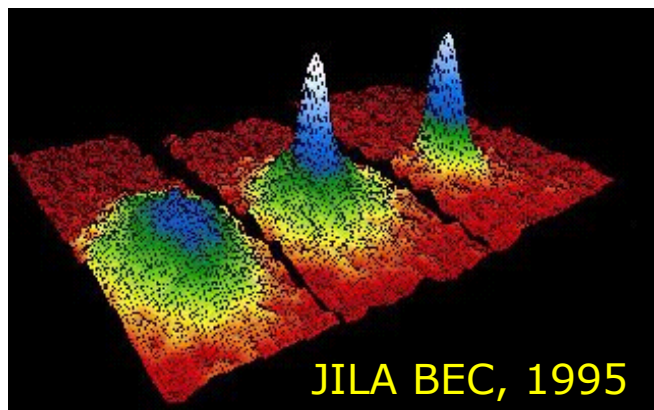
*Under development:*

*2.75"x1.75",  $10^{-8}$  g/Hz<sup>1/2</sup>  
2-axis accelerometer*



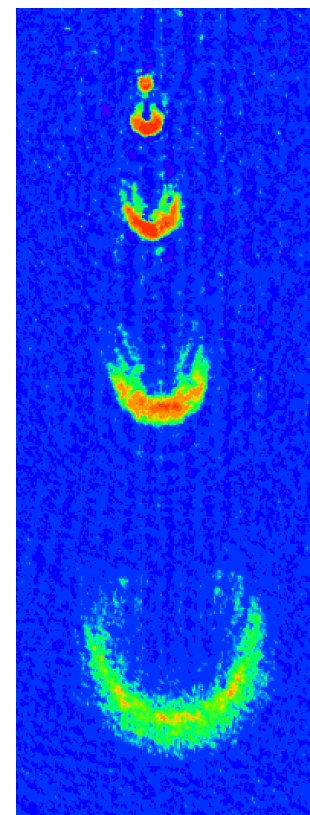
# BEC impact

# Atom lasers



Bose-Einstein  
Condensation of a dilute  
Rb atomic vapor

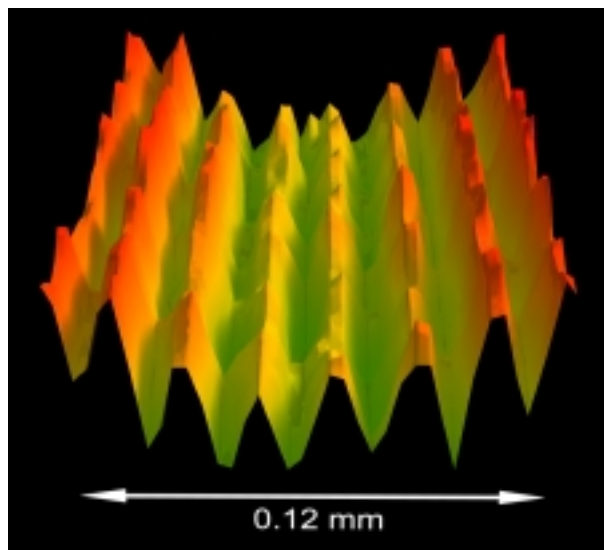
*Revolution in production of bright,  
coherent atomic sources*



1<sup>st</sup> Atom  
Laser, MIT

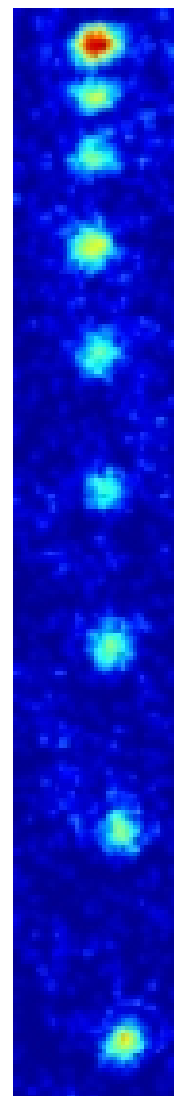


# Atom interferometry with atom lasers



Interference of two overlapping Bose-Einstein condensates: demonstrates analogy with laser light sources (Ketterle, MIT)

*Demonstration of coherence properties and possible applications*



Measurement of  $g$  with a mode-locked atom laser (Yale)

Proof of principle with potential for 1000 x improvement in gravimeter sensitivity.

Pulse output frequency is proportional to  $g$ .

# Next generation atom-optic devices

	Atomic Source	Atom Optics	Read-out
Current Generation	<ul style="list-style-type: none"> <li>• Laser cooled atoms</li> </ul>	<ul style="list-style-type: none"> <li>• Photon recoil</li> <li>• Free-space diffraction grating</li> </ul>	<ul style="list-style-type: none"> <li>• Shot-noise limited</li> </ul>
Next Generation	<ul style="list-style-type: none"> <li>• Atom lasers</li> </ul>	<ul style="list-style-type: none"> <li>• Waveguides</li> </ul>	<ul style="list-style-type: none"> <li>• Quantum correlated state (1/N)</li> </ul>

*Next generation pay-off: compact, ultra-sensitive accelerometer, gyroscopes, clocks*

*Possible 1000x performance gain in next generation sensors*

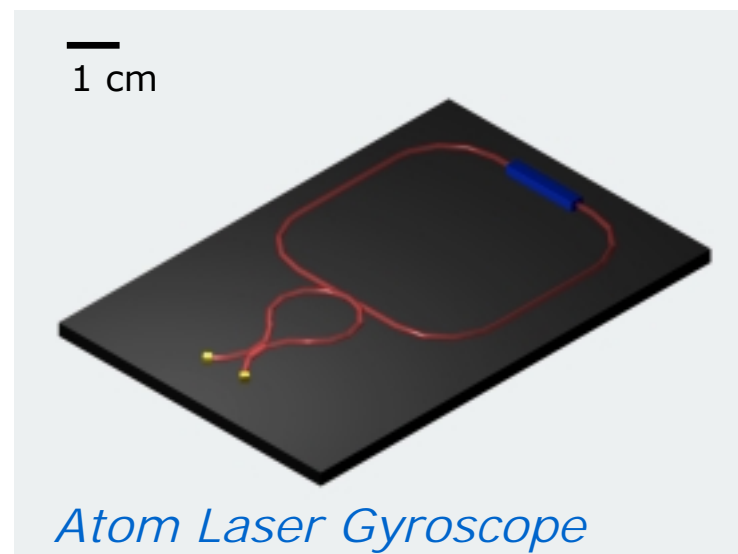
# Waveguide AI sensor types

## Waveguide devices:

Unproven (coherence has yet to be demonstrated!)

Likely very high sensitivity,  
intermediate accuracy.

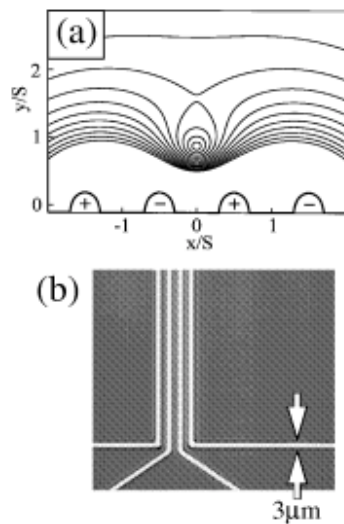
Gyroscope, gravity gradient, and  
accelerometer topologies exist.



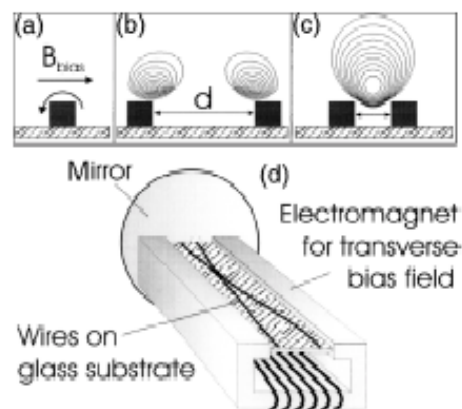
*Technology vision:  
Compact, ultra-sensitive  
(1000x existing sensors),  
inexpensive sensors*

# Atom Waveguides

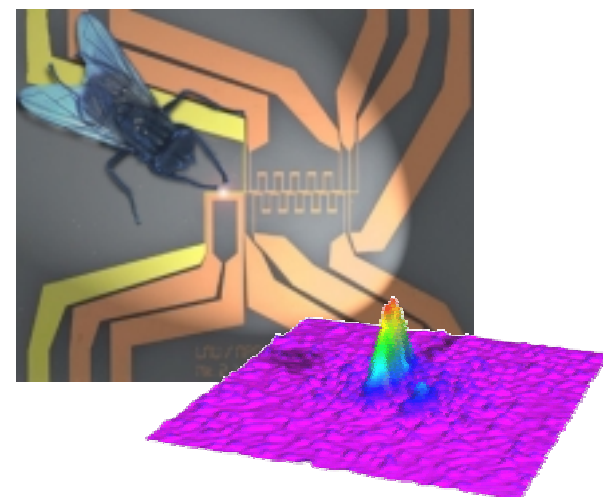
*Basic atom guiding concepts have been demonstrated by several groups.*



Prentiss, Harvard



Anderson, JILA

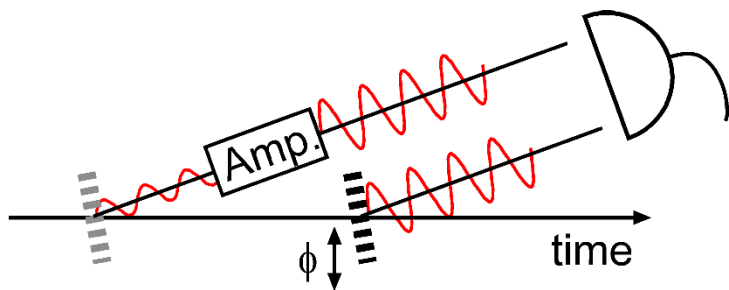


MPQ, Garching

Achieved Bose-Einstein condensation in microtrap.

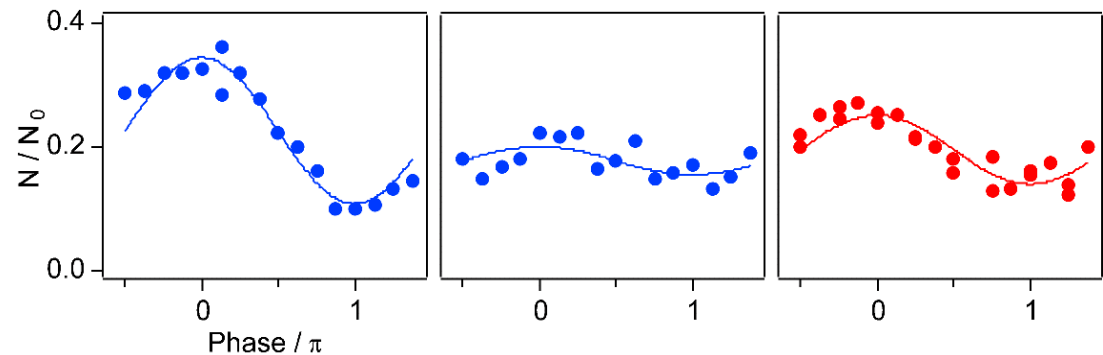
# Matter-wave amplification

## Experiment



Ketterle, MIT

## Results



Interference of an (unamplified) seed pulse with a reference pulse of equal intensity.

A weaker seed pulse led to a reduced fringe contrast.

When the weak seed pulse was amplified, an increase of the fringe contrast provided the proof for the phase-coherence of the atom amplification process

*Laboratory demonstration of coherent matter-wave amplification*

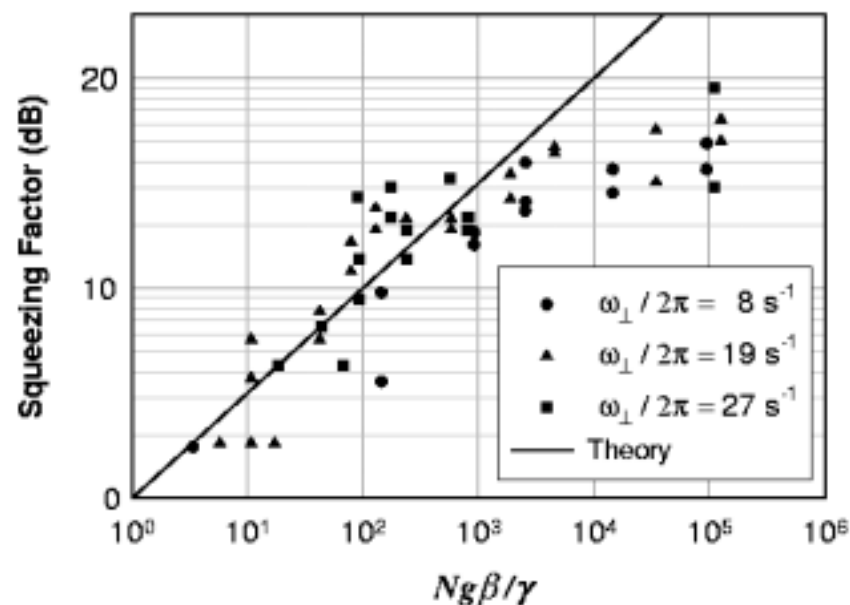
# Atom interferometry with squeezed state atom lasers

Quantum mechanics of many-particle systems allows for measurement sensitivities below the standard (classical) shot-noise limit.

Atom interferometry with squeezed states.

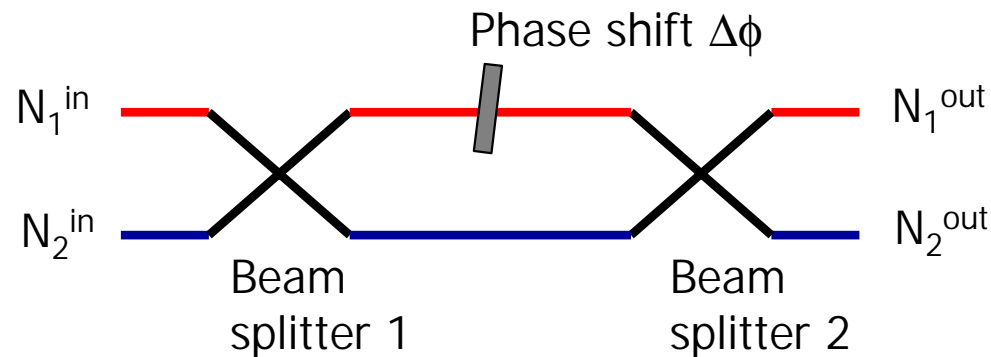
Possible 1000-fold improvement in sensor sensitivity.

*Laboratory demonstration of squeezed-state formation*



# Heisenberg interferometry with degenerate Bose gases

Sub shot-noise interferometry with squeezed/Fock states:  
(following Holland and Burnett, 1993)



Dual Fock state at input  
ports

Number measurements at  
output ports

*Capable of  
resolving phase  
shifts at  
Heisenberg limit  
( $\Delta\phi \sim 1/N$ ).*

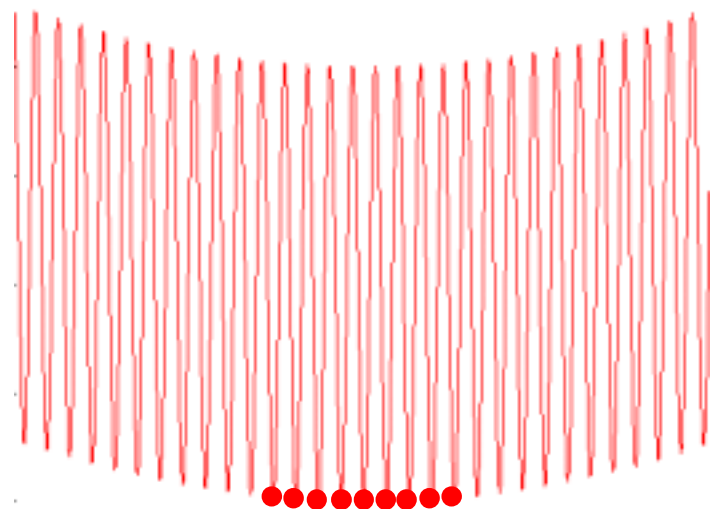
*Possible  
significant gains  
for interferometer  
sensitivity*

Bouyer and Kasevich,  
PRA, 1996 (for BEC  
atoms)

# Correlated atom systems



# BEC in lattice potentials



Our regime:

- 1-D
- 100's of atoms per site,  
10's of lattice sites
- Weak tunneling  
(0.01 – 300 Hz, tunable)
- Strong interactions  
(100 – 500 Hz mean field  
per particle)

Why interesting?

- Quantum states highly correlated/entangled
- Growing links with CM Theory/QPT
- Possible applications to precision measurement/quantum information

This talk

- Ground state properties
- Dynamic response
  - In-situ transport measurements

# Bose-Hubbard Hamiltonian

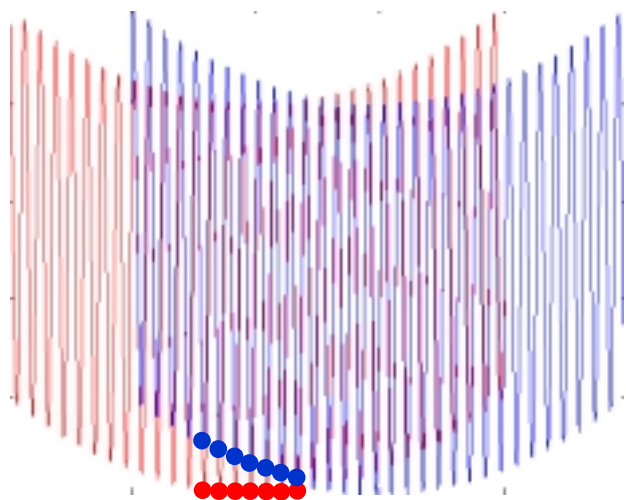
$$H = \gamma \sum_{\langle i,j \rangle} \hat{a}_i^\dagger \hat{a}_j + \frac{1}{2} g \beta_i \sum_i \hat{a}_i^\dagger \hat{a}_i^\dagger \hat{a}_i \hat{a}_i - \sum_i \mu_i \hat{a}_i^\dagger \hat{a}_i$$

tunneling                      mean-field                      external potential

Solve for ground-state and dynamics for  $\sim 3000$  atoms occupying 16 lattice sites in harmonic potential.

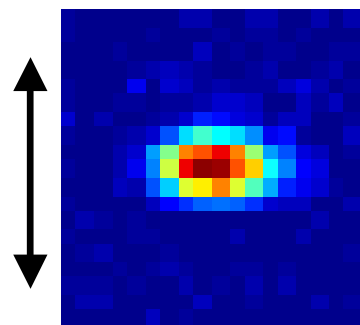
Problem: Hilbert space is huge. Approximations required.

# Transport measurement: Center-of-mass oscillation



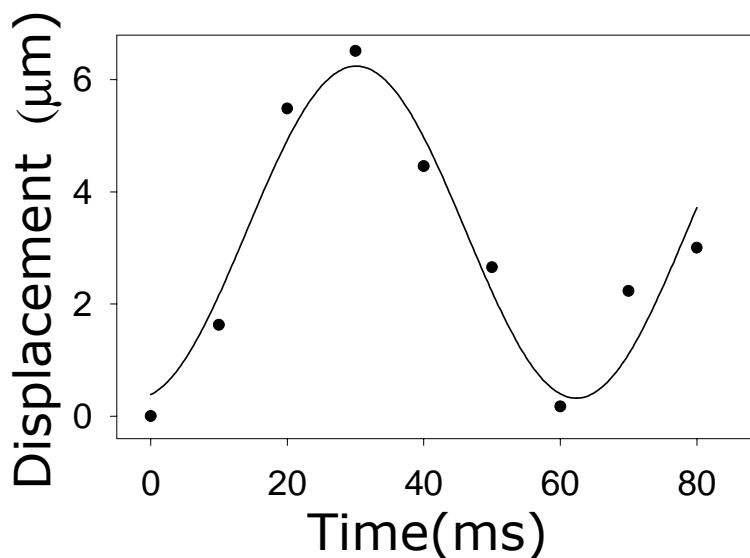
Suddenly displace harmonic potential, leaving corrugated potential fixed.

Observe subsequent dynamic evolution of array center-of-mass (oscillation amplitude and frequency).



*Image of  
lattice array.*

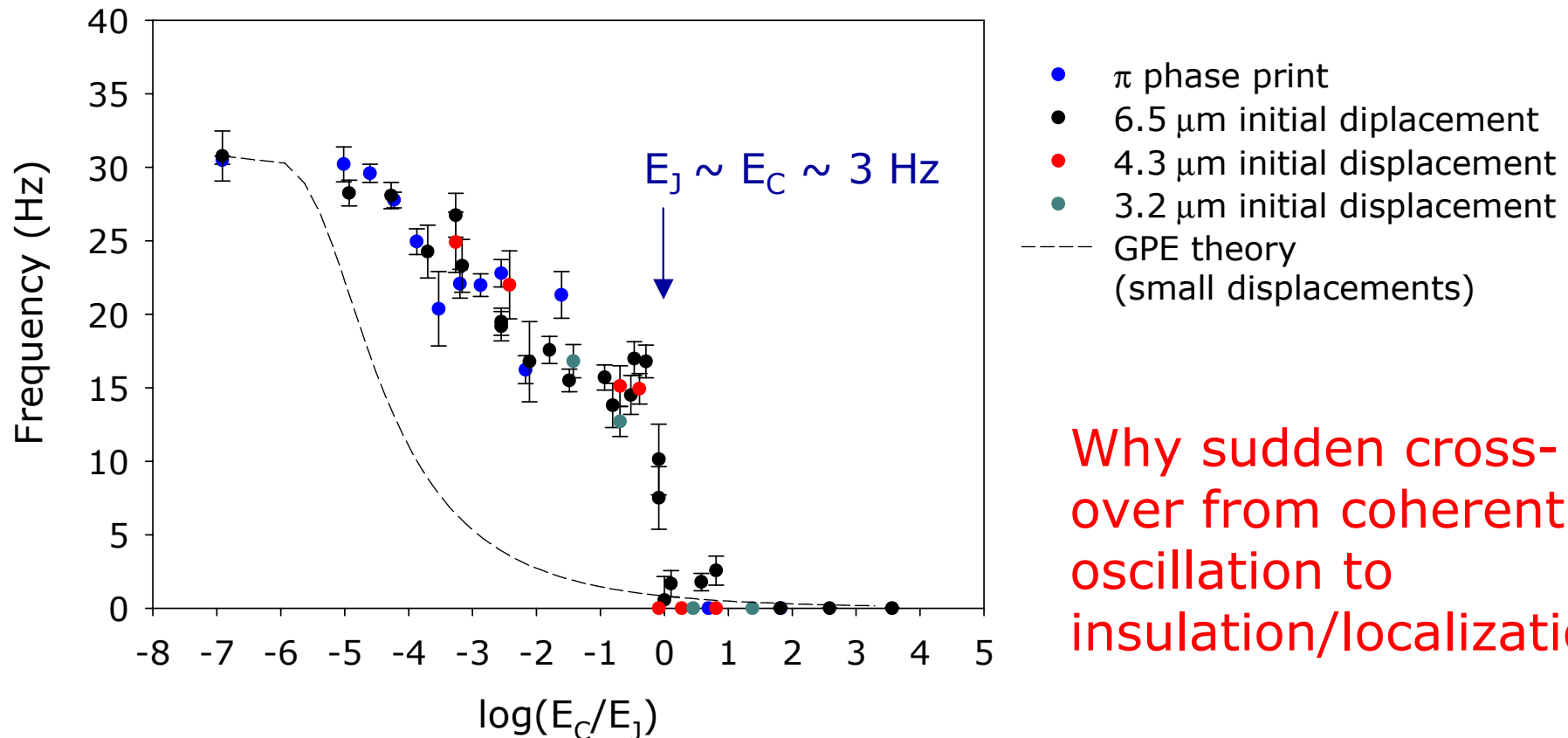
*~ 150 atoms in  
central well.*



# Quantum insulating cross-over

$$E_J \equiv N\gamma = (\# \text{ atoms})(\text{tunneling freq.})$$

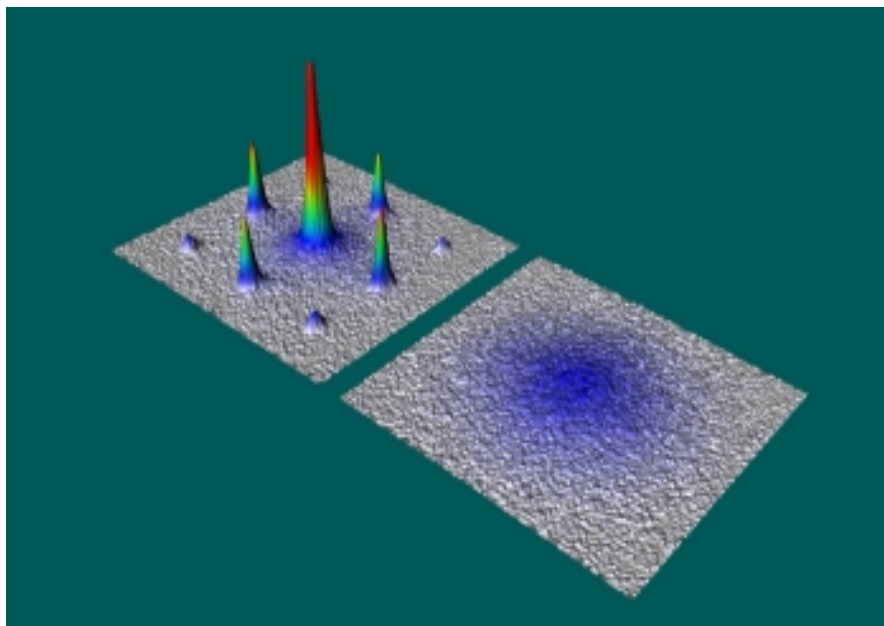
$$E_C \equiv g\beta = (\text{mean field energy per atom})$$



Why sudden cross-over from coherent oscillation to insulation/localization?

# Related work from MPQ

MI transition in 3D optical lattice. Approximately 3 atoms per lattice site.



*I. Bloch, Nature, 2002.*

# Future

- Quantum critical region
  - Quantum phase transitions
- Rotating lattice sites
  - Analog to fractional quantum Hall
- Fermions in lattice
  - High  $T_c$  analog
- QIS
  - Physics-based (use atoms in lattice to understand CM systems)
  - New algorithms for factorization